tive temperature factor' represents not only true thermal vibration but also some spread in position of the atom due to spatial disorder.

Table 3 lists isotropic $B$ values determined in the course of the refinement procedure for the measurements on Schmirntal albite at 20,300 and $600^{\circ} \mathrm{C}$, and on Ramona albite at $-180^{\circ} \mathrm{C}$ (Williams, 1961). When plotted against absolute temperature (Fig. 2) it is seen that for each kind of atom the $B-T$ variation is very closely linear in the range -180 to $300^{\circ} \mathrm{C}$, so that extrapolation to $T=0$ is justified. For sodium, aluminium and silicon atoms the extrapolation gives values of $B$ very close to 0 , whereas for oxygen atoms (at $T=0$ ) $B>0$.
Table 3. Low albite. Isotropic temperature factors $B\left(\AA^{2}\right)$

|  | $(\mathrm{WM}, 1964)$ | $\left(S_{2}\right)$ | $\left(S_{2}\right)$ | $\left(S_{2}\right)$ |
| :--- | :---: | :---: | :--- | :--- |
|  | $-180^{\circ} \mathrm{C}$ | $20^{\circ} \mathrm{C}$ | $300^{\circ} \mathrm{C}$ | $600^{\circ} \mathrm{C}$ |
| Na | $1.0(3)$ | $3.2(1)$ | $5 \cdot 6(1)$ | $6.7(2)$ |
| Al | $0.15(6)$ | $0.72(6)$ | $1.04(9)$ | $1 \cdot 1(1)$ |
| Al (average) | $0.18(6)$ | $0.63(4)$ | $0.94(6)$ | $1.20(8)$ |
| O (average) | $0.38(6)$ | $1.01(6)$ | $1.65(7)$ | $2.0(1)$ |

Notes. Standard deviations are in brackets and refer to the last figure given.
Measurements on Schmirntal second fragment ( $S_{2}$ ) and from Williams \& Megaw (1964).

The difference between $\mathrm{Na}, \mathrm{Al}$ and Si on the one hand, and O on the other, may be taken as evidence in support of a model in which the position of the Na atom is as clearly defined as are the positions of Al and Si atoms at the centres of their tetrahedral groups. Its large anisotropy is then due to anisotropic thermal vibration, not to positional disorder. By contrast, the O atoms show some positional disorder arising from the differences in $\mathrm{Si}-\mathrm{O}$ and $\mathrm{Al}-\mathrm{O}$ bond lengths and incomplete $\mathrm{Al}, \mathrm{Si}$ order.

## 6. Conclusion

Measurements of diffraction intensities from low albite at 300 and $600^{\circ} \mathrm{C}$ have been used to study the anisotropy of the sodium atom as seen in [100] projection. Comparison with previous studies at room temperature and at $-180^{\circ} \mathrm{C}$ provides strong support for the view that the observed anisotropy represents a true anisotropic thermal vibration of the sodium atom.

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# The Molecular and Crystal Structure of Hippuric Acid 

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Hippuric acid, $\mathrm{C}_{6} \mathrm{H}_{5} . \mathrm{CO} . \mathrm{NH} . \mathrm{CH}_{2} . \mathrm{COOH}$, crystallizes with four molecules in an orthorhombic unit cell with $a=8.874, b=10.577, c=9 \cdot 117 \AA$, space group $P 2_{1} 2_{1} 2_{1}$. The structure has been determined by direct methods and refined by full-matrix least-squares computations. The final $R$ value is $5 \cdot 8 \%$. The benzene ring, the peptide part and the carboxylic group are planar and twisted with respect to each other. The molecules are held together in three dimensions by one $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ and one $\mathrm{N}-\mathrm{H} \cdots \mathrm{O}$ hydrogen bond to the peptide oxygen atom.

## Introduction

Hippuric acid


is formed in mammals when benzoic acid is detoxicated by conjugation with glycine. It is excreted in urine and constitutes about a half per cent of the nitrogen excretion in man. The crystallographic and optical data of hippuric acid have been given by Ringertz (1969).

## Experimental

Commercially available hippuric acid was recrystallized in water. The cell axes $a$ and $b$ were determined
from photographic measurements of high-angle reflexions with $\mathrm{Cu} K \alpha$ radiation ( $\lambda_{k \alpha 1}=1 \cdot 54051 \AA$ ). The $c$ axis was determined with a Philips automatic singlecrystal diffractometer PAILRED using Mo $K \alpha$ radia-

Table 1. Final observed and calculated structure factors
The sign * represents a 'less than' reflexion. The columns are $l, 10 F_{o}, 10 F_{c}, 10 A$ and $10 B$.



Fig.1. Diagrams showing bond lengths and angles in the hippuric acid molecule.
tion. The following dimensions of the orthorhombic unit-cell were observed. The refractive indices refer to the crystallographic axes.

$$
\begin{array}{ll}
a=8.874 \pm 2 \AA & \beta=1.592^{\circ} \\
b=10.577 \pm 3 & \gamma=1.760 \\
c=9.117 \pm 3 & \alpha=1.535
\end{array}
$$

Systematic absences were $h 00,0 k 0$ and $00 l$ with $h, k$ and $l$ respectively equal to $2 n+1$, space group $P 2_{1} 2_{1} 2_{1} . D_{\text {obs }}=1.385 \mathrm{~g} . \mathrm{cm}^{-3}$ and $D_{\text {calc }}=1.390 \mathrm{~g} . \mathrm{cm}^{-3}$, assuming $Z=4$. Two sets of reflexion data were recorded using two small crystals measuring approximately $0.15 \times 0.15 \times 0.15 \mathrm{~mm}$. The first data set was collected using Ni -filtered $\mathrm{Cu} K \alpha$ radiation and a General Electric single-crystal orienter which was operated manually. The second set of data was collected with a Philips automatic single-crystal diffractometer, PAIL-

RED, using monochromatized Mo $K \alpha$ radiation. In the first case 1098 structure amplitudes were obtained of which the 112 weakest were regarded as not observable. The two sets of data were corrected for Lorentz and polarization factors and put on an absolute scale. It was found that there was strong extinction of the most intense reflexions in the first data set and accordingly the 25 highest structure amplitudes were taken from the second data set. The $E$ values were then calculated, giving the following statistical averages

|  | $\{\|E\|\}$ | $\{\|E\|\}$ | $\left\{\left\|E^{2}-1\right\|\right\}$ |
| :--- | :---: | :---: | :---: |
| Observed | 0.840 | 1.000 | 0.797 |
| Theoretical for acentric | 0.886 | 1.000 | 0.736 |
| Theoretical for centric | 0.798 | 1.000 | 0.968 |

## Structure determination

The determination of the structure took four years and most crystallographic methods have been applied. However the optical indicatrix and the strength of the 102 and 202 reflexions indicated planar molecules with all parts parallel to the $b$ axis and with the molecules inclined about $70^{\circ}$ to each other. Spherical Patterson sections at 1.4 and 2.4 could be explained in detail by an essentially planar molecular model. In retrospect all assumptions were found to have been correct except that the carboxyl group was inclined at $85^{\circ}$ with respect to the rest of the molecule and not coplanar with it.

The structure was finally solved using direct methods in a computer program series, GAASA 1-7 (Lindgren, Lindqvist \& Nyborg, 1970). 273 reflexions with $E \geq 1 \cdot 2$ were used in a symbolic addition procedure having a basic set of 10 symbols which were given to the strongest normalized structure factors taking part in the largest number of Sayre triplets. The number of symbols was then reduced on a statistical basis until 4 were left after 7 cycles:


Fig.2. Thermal ellipsoid representation of a hippuric acid molecule showing the labelling of the atoms. The ellipsoids enclose $50 \%$ probability. The hydrogen atoms are indicated by small spheres.

| $h$ | $k$ | $l$ | $E$ | Phase |
| ---: | ---: | ---: | :---: | :---: |
| 5 | 0 | 6 | 3.1 | 0 |
| 8 | 7 | 0 | $2 \cdot 9$ | 0 |
| 0 | 7 | 5 | $2 \cdot 7$ | $\pi$ |
| 1 | 12 | 5 | $2 \cdot 6$ | $\pi$ |

These symbols were then given the above tabulated phase values to fix the origin and the enantiomorph. From the given values 152 preliminary phases were calculated and an iterative use of the tangent formula (Karle \& Hauptman, 1956) was started. At the end of these calculations an $E$ value map was calculated from all 273 phases and then automatically scanned for peaks. From the 22 highest peaks two geometrically perfect molecular arrangements could be found. These two models were perfectly alike and related to each other by a $1.4 \AA$ translation along the $b$ axis. None of the two molecular positions converged, however, when refined by least-squares methods. When hydrogen bonding possibilities were taken into consideration the position exactly between the two was refined to $R=$ $14 \%$ after 3 cycles.

## Refinement of the structure

Introduction of anisotropic temperature factors reduced the $R$ value to $9.8 \%$. At this stage a difference synthesis was performed revealing all nine hydrogen atom positions. The hydrogen positional parameters were refined but the hydrogen atoms were given the same anisotropic temperature factors as that of the covalently bonded 'heavy' atom. A weighting scheme of the form $w=1 /\left(3+F_{o}+F_{o}^{2} / 55\right)$ (Cruickshank, 1965, p. 114) was used. The final $R$ value obtained after two


Fig.3. Drawing of the crystal structure projected along the $a$ axis showing the hydrogen bonding system.
additional cycles was $5 \cdot 8 \%$. The average and maximum positional shifts of the non-hydrogen atoms in the final cycle were 23 and $72 \%$ respectively of the estimated standard deviations. Observed and calculated structure factors are listed in Table 1.

## Results and discussion

## Molecular arrangement

The hippuric acid molecule is not extended to its maximum length. The carboxyl group has been rotated around the $\mathrm{N}-\mathrm{C}(8)$ bond forming an approximate right angle with the rest of the molecule. This brings one of the carboxyl oxygen atoms into a hydrogen bonding position with respect to the peptide oxygen atom in the molecule related to the original by the

Table 2. Final fractional atomic positional parameters and anisotropic temperature factor parameters, all with estimated standard errors

The thermal parameters are in the form: $\exp \left(-\beta_{11} h^{2}-\beta_{22} k^{2}-\beta_{33} l^{2}-2 \beta_{12} h k-2 \beta_{23} k l-2 \beta_{13} h l\right)$.

|  | $x / a$ | $\sigma$ | $y / b$ | $\sigma$ | z/c | $\sigma$ | $\beta_{11}$ | $\sigma$ | $\beta_{22}$ | $\sigma$ | $\beta_{33}$ | $\sigma$ | $\beta_{12}$ | $\sigma$ | $\beta_{13}$ | $\sigma$ | $\beta_{23}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| O(1) | 1164 | 4 | 5256 | 3 | 10275 | 3 | 123 | 5 | 59 | 3 | 78 | 4 | 12 | 3 | 14 | 4 | -10 |
| O(2) | 4628 | 4 | 6634 | 3 | 9341 | 5 | 119 | 5 | 67 | 3 | 172 | 6 | 10 | 4 | -53 | 5 | 1 |
| $\mathrm{O}(3)$ | 3726 | 4 | 8527 | 3 | 8717 | 4 | 111 | 5 | 49 | 3 | 150 | 5 | -5 | 3 | -33 | 5 | 1 |
| N | 2131 | 5 | 5433 | 3 | 8009 | 4 | 100 | 5 | 49 | 3 | 74 | 4 | -9 | 3 | 2 | 5 | -3 |
| C(1) | 1460 | 5 | 3364 | 4 | 8897 | 5 | 71 | 5 | 48 | 3 | 77 | 5 | 1 | 4 | -9 | 5 | -1 |
| C(2) | 2200 | 6 | 2711 | 4 | 7761 | 5 | 106 | 6 | 54 | 4 | 99 | 6 | -3 | 4 | 14 | 6 | -4 |
| C(3) | 2070 | 6 | 1409 | 4 | 7674 | 6 | 122 | 7 | 53 | 4 | 128 | 7 | 6 | 5 | 11 | 7 | -9 |
| C(4) | 1221 | 6 | 739 | 4 | 8709 | 6 | 102 | 6 | 54 | 4 | 146 | 8 | -2 | 5 | -13 | 7 | 4 |
| C(5) | 479 | 6 | 1382 | 4 | 9826 | 6 | 105 | 7 | 65 | 4 | 127 | 7 | -8 | 5 | 6 | 6 | 22 |
| C(6) | 587 | 5 | 2697 | 4 | 9924 | 6 | 98 | 6 | 61 | 4 | 95 | 6 | -9 | 4 | 6 | 5 | 3 |
| C(7) | 1575 | 4 | 4763 | 4 | 9111 | 5 | 67 | 5 | 51 | 3 | 78 | 5 | 1 | 4 | -10 | 4 | -2 |
| C(8) | 2215 | 6 | 6823 | 4 | 8105 | 6 | 90 | 6 | 46 | 4 | 110 | 6 | 1 | 4 | -5 | 6 | 4 |
| C(9) | 3668 | 5 | 7274 | 4 | 8798 | 5 | 97 | 6 | 53 | 4 | 87 | 5 | 0 | 4 | 2 | 6 | -4 |
| H(1) | 2939 | 71 | 3224 | 55 | 7044 | 64 |  |  |  |  |  |  |  |  |  |  |  |
| H(2) | 2561 | 68 | 945 | 54 | 6702 | 75 |  |  |  |  |  |  |  |  |  |  |  |
| H(3) | 1075 | 68 | -192 | 54 | 8559 | 72 |  |  |  |  |  |  |  |  |  |  |  |
| H(4) | -177 | 69 | 1072 | 53 | 10691 | 72 |  |  |  |  |  |  |  |  |  |  |  |
| H(5) | -238 | 68 | 3157 | 51 | 10643 | 66 |  |  |  |  |  |  |  |  |  |  |  |
| H(6) | 2124 | 70 | 5308 | 54 | 7045 | 70 |  |  |  |  |  |  |  |  |  |  |  |
| H(7) | 1880 | 70 | 7214 | 55 | 7035 | 69 |  |  |  |  |  |  |  |  |  |  |  |
| H(8) | 1306 | 70 | 7155 | 53 | 8660 | 68 |  |  |  |  |  |  |  |  |  |  |  |
| H(9) | 4388 | 74 | 8794 | 56 | 9107 | 78 |  |  |  |  |  |  |  |  |  |  |  |

Table 3. Distances and angles of the hippuric acid molecule, with estimated standard deviations

| Non-hydrogen intramolecular distances |  |
| :---: | :---: |
| $\mathrm{C}(1)-\mathrm{C}(2)$ | $1 \cdot 407$ (7) $\AA$ |
| $\mathrm{C}(1)-\mathrm{C}(6)$ | $1 \cdot 405$ (6) |
| $\mathrm{C}(1)-\mathrm{C}(7)$ | 1.496 (6) |
| $\mathrm{C}(2)-\mathrm{C}(3)$ | $1 \cdot 384$ (6) |
| $\mathrm{C}(3)-\mathrm{C}(4)$ | $1 \cdot 400$ (8) |
| $\mathrm{C}(4)-\mathrm{C}(5)$ | $1 \cdot 391$ (8) |
| $\mathrm{C}(5)-\mathrm{C}(6)$ | 1.396 (7) |
| $\mathrm{C}(8)-\mathrm{C}(9)$ | 1.513 (7) |
| $\mathrm{C}(7)-\mathrm{N}$ | 1.336 (6) |
| $\mathrm{C}(8)-\mathrm{N}$ | 1.454 (6) |
| $\mathrm{C}(7)-\mathrm{O}(1)$ | $1 \cdot 238$ (5) |
| $\mathrm{C}(9)-\mathrm{O}(2)$ | $1 \cdot 196$ (6) |
| $\mathrm{C}(9)-\mathrm{O}(3)$ | 1.328 (5) |

Angles involving non-hydrogen atoms

| $\mathrm{C}(2)-\mathrm{C}(1)-\mathrm{C}(6)$ | $120 \cdot 1(4)^{\circ}$ |
| :--- | :--- |
| $\mathrm{C}(2)-\mathrm{C}(1)-\mathrm{C}(7)$ | $123 \cdot 3(4)$ |
| $\mathrm{C}(6)-\mathrm{C}(1)-\mathrm{C}(7)$ | $116 \cdot 6(4)$ |
| $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{C}(3)$ | $119 \cdot 5(5)$ |
| $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{C}(4)$ | $120 \cdot 6(5)$ |
| $\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{C}(5)$ | $120.1(4)$ |
| $\mathrm{C}(4)-\mathrm{C}(5)-\mathrm{C}(6)$ | $120 \cdot 1(5)$ |
| $\mathrm{C}(5)-\mathrm{C}(6)-\mathrm{C}(1)$ | $119 \cdot 7(4)$ |
| $\mathrm{C}(1)-\mathrm{C}(7)-\mathrm{N}$ | $117 \cdot 9(4)$ |
| $\mathrm{C}(1)-\mathrm{C}(7)-\mathrm{O}(1)$ | $120.6(4)$ |
| $\mathrm{N}--\mathrm{C}(7)-\mathrm{O}(1)$ | $12 \cdot 5(4)$ |
| $\mathrm{C}(7)-\mathrm{N}--\mathrm{C}(8)$ | $121 \cdot 2(4)$ |
| $\mathrm{N}--\mathrm{C}(8)-\mathrm{C}(9)$ | $112 \cdot 5(4)$ |
| $\mathrm{C}(8)-\mathrm{C}(9)-\mathrm{O}(2)$ | $127 \cdot 0(4)$ |
| $\mathrm{C}(8)-\mathrm{C}(9)-\mathrm{O}(3)$ | $108 \cdot 9(4)$ |
| $\mathrm{O}(2)-\mathrm{C}(9)-\mathrm{O}(3)$ | $124 \cdot 1(4)$ |

twofold screw axis parallel to the $a$ axis. The molecules are further held together by a $\mathrm{N}-\mathrm{H} \cdots \mathrm{O}$ hydrogen bond to the peptide oxygen atom in the $c$ axis screwrelated molecule. The molecules are oriented with their long dimension essentially parallel to the $b$ axis with the non-carboxyl parts of the molecule tilted about $35^{\circ}$ with respect to the (100) plane. The molecular arrangement can be seen in Fig. 1.

## Molecular structure

The labelling and the thermal displacement ellipsoids of the atoms can be seen in Fig. 2 and the final positional and vibrational parameters in Table 2. From these values the interatomic distances and angles have been calculated and they are shown in Fig. 3, and are shown together with their estimated standard deviations in Table 3. The root-mean-square components of thermal displacement along the three principal axes are tabulated in Table 4 together with the angles between these principal axes and the unit-cell axes.

The configuration of the molecule is in agreement with earlier structure determinations on similar structures. Compared with the structure of N -acetylglycine, $\mathrm{CH}_{3} . \mathrm{CO} . \mathrm{NH} . \mathrm{CH}_{2} . \mathrm{COOH}$ (Carpenter \& Donohue, 1950) the average deviations for comparable nonhydrogen bond lengths and angles are $0.008 \AA$ and $1 \cdot 3^{\circ}$ respectively and no single deviation is significant. The dimensions of the peptide part of the molecule are in relatively good agreement with the averaged values given by Marsh \& Donohue (1967). In this case the

| Distances to hydrogen atoms |  |
| :---: | :---: |
| $\mathrm{C}(2)-\mathrm{H}(1)$ | 1.07 (6) $\AA$ |
| $\mathrm{C}(3)-\mathrm{H}(2)$ | $1 \cdot 10$ (7) |
| $\mathrm{C}(4)-\mathrm{H}(3)$ | 1.00 (6) |
| $\mathrm{C}(5)-\mathrm{H}(4)$ | 1.03 (6) |
| $\mathrm{C}(6)-\mathrm{H}(5)$ | $1 \cdot 10$ (6) |
| $\mathrm{N}-\mathrm{H}(6)$ | $0 \cdot 89$ (6) |
| $\mathrm{C}(8)-\mathrm{H}(7)$ | $1 \cdot 10$ (6) |
| $\mathrm{C}(8)-\mathrm{H}(8)$ | 1.02 (6) |
| $\mathrm{O}(3)-\mathrm{H}(9)$ | 0.74 (7) |
| Angles <br> involving hydrogen atoms |  |
|  |  |
| $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{H}(1)$ | 119 (3) ${ }^{\circ}$ |
| $\mathrm{C}(3)-\mathrm{C}(2)-\mathrm{H}(1)$ | 121 (3) |
| $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{H}(2)$ | 117 (3) |
| $\mathrm{C}(4)-\mathrm{C}(3)-\mathrm{H}(2)$ | 122 (3) |
| $\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{H}(3)$ | 118 (4) |
| $\mathrm{C}(5)-\mathrm{C}(4)-\mathrm{H}(3)$ | 121 (4) |
| $\mathrm{C}(4)-\mathrm{C}(5)-\mathrm{H}(4)$ | 132 (3) |
| $\mathrm{C}(6)-\mathrm{C}(5)-\mathrm{H}(4)$ | 108 (3) |
| $\mathrm{C}(5)-\mathrm{C}(6)-\mathrm{H}(5)$ | 116 (3) |
| $\mathrm{C}(1)-\mathrm{C}(6)-\mathrm{H}(5)$ | 123 (3) |
| $\mathrm{C}(7)-\mathrm{N}-\mathrm{H}(6)$ | 130 (4) |
| $\mathrm{C}(8)-\mathrm{N}-\mathrm{H}(6)$ | 103 (4) |
| $\mathrm{N}-\mathrm{C}(8)-\mathrm{H}(7)$ | 108 (3) |
| $\mathrm{C}(9)-\mathrm{C}(8)-\mathrm{H}(7)$ | 119 (3) |
| $\mathrm{N}-\mathrm{C}(8)-\mathrm{H}(8)$ | 109 (3) |
| $\mathrm{C}(9)-\mathrm{C}(8)-\mathrm{H}(8)$ | 111 (3) |
| $\mathrm{H}(7)-\mathrm{C}(8)-\mathrm{H}(8)$ | 96 (5) |
| $\mathrm{C}(9)-\mathrm{O}(3)-\mathrm{H}(9)$ | 113 (5) |

mean deviations for bonds and angles are $0.006 \AA$ and $1.3^{\circ}$ respectively. The benzene ring has a normal configuration with an average aromatic $\mathrm{C}-\mathrm{C}$ bond length of $1.397 \AA$.

## The least-squares planes of the structure

Table 5 shows some least-squares planes calculated through the molecule including only non-hydrogen atoms given equal weight. In the benzene ring (plane I) none of the atoms deviates more than $0.005 \AA$ and that part is accordingly perfectly planar within the experimental error. The significant deviations of the atoms from planarity in the peptide (plane II) and carboxyl (plane III) planes depends essentially on the $\mathrm{N}-\mathrm{C}(8)$ bond which deviates from both of these planes.

The twist of the molecule can be described in terms of two rotations in the same direction. The peptide plane (plane II) is rotated $14^{\circ}$ with respect to the benzene ring (plane I) and the carboxyl group (plane III) $83^{\circ}$ with respect to the peptide group. The rotations are around the $\mathrm{C}(1)-\mathrm{C}(7)$ and $\mathrm{N}-\mathrm{C}(8)$ bonds respectively.

## Hydrogen bonding

Both available non-carbon-bonded hydrogen atoms are involved in hydrogen bonds to the peptide oxygen atom. This is demonstrated in Fig. 1 and the distances and angles involved are tabulated in Table 6. The $\mathrm{N}-\mathrm{H} \cdots \mathrm{O}$ bond $(3.01 \AA)$ thus connects the molecules forming infinite rows along the $c$ axis and the $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$

Table 4. Principal axes (i) of anisotropic temperature factors, referred to the crystallographic axes ABC
The r.m.s. displacements $\bar{\mu}_{i}$ are in $\AA$ and the direction angles, $V$, are in degrees.

|  | $i$ | $\bar{\mu}_{i}$ | $\sigma$ | $V_{a}$ | $\sigma$ | $V_{b}$ | $\sigma$ | $V_{c}$ | $\sigma$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mathrm{O}(1)$ | 1 | $0 \cdot 160$ | 5 | 71 | 3 | 131 | 5 | 48 | 5 |
|  | 2 | $0 \cdot 195$ | 5 | 91 | 6 | 45 | 6 | 45 | 6 |
|  | 3 | $0 \cdot 228$ | 4 | 161 | 3 | 104 | 5 | 77 | 5 |
| $\mathrm{O}(2)$ | 1 | $0 \cdot 179$ | 6 | 135 | 6 | 54 | 9 | 67 | 4 |
|  | 2 | $0 \cdot 202$ | 5 | 61 | 8 | 36 | 9 | 109 | 4 |
|  | 3 | $0 \cdot 292$ | 5 | 60 | 2 | 87 | 2 | 31 | 2 |
| $\mathrm{O}(3)$ | 1 | $0 \cdot 164$ | 5 | 100 | 8 | 169 | 8 | 87 | 4 |
|  | 2 | $0 \cdot 193$ | 5 | 30 | 4 | 100 | 8 | 117 | 3 |
|  | 3 | $0 \cdot 265$ | 5 | 62 | 3 | 92 | 2 | 28 | 3 |
| N | 1 | $0 \cdot 162$ | 6 | 106 | 7 | 158 | 10 | 76 | 16 |
|  | 2 | $0 \cdot 177$ | 6 | 101 | 11 | 102 | 16 | 164 | 15 |
|  | 3 | $0 \cdot 203$ | 5 | 160 | 7 | 72 | 6 | 83 | 11 |
| $\mathrm{C}(1)$ | 1 | $0 \cdot 162$ | 7 | 61 | 11 | 86 | 13 | 29 | 11 |
|  | 2 | $0 \cdot 165$ | 6 | 148 | 33 | 75 | 86 | 63 | 22 |
|  | 3 | $0 \cdot 186$ | 6 | 78 | 75 | 16 | 83 | 101 | 41 |
| $\mathrm{C}(2)$ | 1 | $0 \cdot 173$ | 6 | 92 | 14 | 171 | 11 | 81 | 14 |
|  | 2 | $0 \cdot 190$ | 7 | 135 | 9 | 95 | 18 | 135 | 10 |
|  | 3 | $0 \cdot 219$ | 7 | 135 | 9 | 82 | 6 | 46 | 9 |
| $\mathrm{C}(3)$ | 1 | $0 \cdot 169$ | 7 | 79 | 6 | 165 | 7 | 79 | 5 |
|  | 2 | $0 \cdot 218$ | 7 | 30 | 15 | 75 | 7 | 64 | 15 |
|  | 3 | $0 \cdot 238$ | 7 | 118 | 15 | 85 | 6 | 29 | 14 |
| $\mathrm{C}(4)$ | 1 | $0 \cdot 174$ | 6 | 93 | 14 | 176 | 8 | 93 | 5 |
|  | 2 | $0 \cdot 199$ | 6 | 14 | 7 | 92 | 14 | 104 | 6 |
|  | 3 | $0 \cdot 250$ | 7 | 76 | 6 | 93 | 4 | 14 | 6 |
| $\mathrm{C}(5)$ | 1 | $0 \cdot 173$ | 7 | 110 | 9 | 147 | 6 | 115 | 5 |
|  | 2 | $0 \cdot 209$ | 7 | 20 | 9 | 109 | 9 | 98 | 9 |
|  | 3 | $0 \cdot 243$ | 7 | 91 | 9 | 116 | 5 | 26 | 5 |
| $\mathrm{C}(6)$ | 1 | $0 \cdot 177$ | 7 | 122 | 11 | 143 | 13 | 107 | 13 |
|  | 2 | $0 \cdot 199$ | 7 | 111 | 33 | 59 | 20 | 141 | 36 |
|  | 3 | $0 \cdot 206$ | 7 | 140 | 23 | 72 | 23 | 56 | 37 |
| $\mathrm{C}(7)$ | 1 | $0 \cdot 158$ | 6 | 154 | 9 | 86 | 24 | 64 | 10 |
|  | 2 | $0 \cdot 170$ | 5 | 90 | 23 | 10 | 19 | 100 | 19 |
|  | 3 | $0 \cdot 187$ | 6 | 64 | 9 | 81 | 17 | 27 | 10 |
| $\mathrm{C}(8)$ | 1 | $0 \cdot 162$ | 7 | 87 | 11 | 174 | 8 | 95 | 6 |
|  | 2 | $0 \cdot 189$ | 6 | 11 | 12 | 86 | 11 | 101 | 12 |
|  | 3 | $0 \cdot 217$ | 6 | 79 | 12 | 95 | 6 | 12 | 11 |
| $\mathrm{C}(9)$ | 1 | $0 \cdot 172$ | 6 | 89 | 13 | 165 | 14 | 75 | 14 |
|  | 2 | $0 \cdot 192$ | 6 | 110 | 54 | 104 | 15 | 155 | 44 |
|  | 3 | $0 \cdot 198$ | 6 | 160 | 53 | 87 | 18 | 71 | 52 |
|  |  |  |  |  |  |  |  |  |  |

Table 5. Equations of some least-squares planes in the hippuric acid molecule and the distances of the atoms from these planes
Equations are expressed in the form $l A+m B+n C=D$ where $A, B, C$ and $D$ are in $\AA$ and $A, B$ and $C$ are along the crystallo-


Table 6. Some distances and angles involved in the hydrogen bonds

| Donor | Acceptor | Hydrogen | $X-\mathrm{H} \cdots \mathrm{O}$ | $\sigma$ | $\mathrm{H} \cdots \mathrm{O}$ | $\sigma$ | $X-\mathrm{H}-\mathrm{O}$ | $\sigma$ |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| N | $\mathrm{O}(1)\left(\frac{1}{2}-x ; 1-y ; z-\frac{1}{2}\right)$ | $\mathrm{H}(6)$ | 3.011 | 6 | $2.30 \AA$ | 6 | $137^{\circ}$ | 5 |
| $\mathrm{O}(3)$ | $\mathrm{O}(1)\left(\frac{1}{2}+x ; 1 \frac{1}{2}-y ; 2-z\right)$ | $\mathrm{H}(9)$ | 2.680 | 6 | 1.95 | 6 | 166 | 6 |

bonds $(2.68 \AA$ ) connect the molecules in infinite rows along the $a$ axis. Together these two hydrogen bonds form a stabilized three-dimensional intermolecular network.

The proposed intramolecular hydrogen bond for hippuric acid in solution (Schätzle \& Rottenberg, 1963) between the unprotonized carboxyl oxygen atom and the nitrogen atom is found to be sterically impossible in the solid state.

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# The Crystal Structure of Disodium Dihydrogen Hypophosphate Hexahydrate $\left(\mathrm{Na}_{2} \mathrm{H}_{2} \mathrm{P}_{2} \mathrm{O}_{6} \cdot \mathbf{6} \mathrm{H}_{2} \mathrm{O}\right)$ and <br> Disodium Dihydrogen Pyrophosphate Hexahydrate ( $\mathrm{Na}_{2} \mathbf{H}_{2} \mathbf{P}_{\mathbf{2}} \mathrm{O}_{7.6} \mathbf{H}_{2} \mathrm{O}$ ) 

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#### Abstract

The crystal structures of the isomorphous disodium hypophosphate hexahydrate $\left(\mathrm{Na}_{2} \mathrm{H}_{2} \mathrm{P}_{2} \mathrm{O}_{6} \cdot 6 \mathrm{H}_{2} \mathrm{O}\right)$ and disodium dihydrogen pyrophosphate hexahydrate $\left(\mathrm{Na}_{2} \mathrm{H}_{2} \mathrm{P}_{2} \mathrm{O}_{7} \cdot 6 \mathrm{H}_{2} \mathrm{O}\right)$ have been determined with diffractometer data. The space group is $C 2 / c$ and a unit cell contains four formula units. The unit-cell dimensions of $\mathrm{Na}_{2} \mathrm{H}_{2} \mathrm{P}_{2} \mathrm{O}_{6} .6 \mathrm{H}_{2} \mathrm{O}$ are $a=14.090$ (3), $b=6.998$ (1), $c=12.700$ (6) $\AA, \beta=115.94$ (2) ${ }^{\circ}$ and those of $\mathrm{Na}_{2} \mathrm{H}_{2} \mathrm{P}_{2} \mathrm{O}_{7} .6 \mathrm{H}_{2} \mathrm{O}$ are $a=14.099$ (6), $b=6.959$ (4), $c=13.455$ (8) $\AA, \beta=117.69$ (4) ${ }^{\circ}$. The hypophosphate ion has $C_{2}$ symmetry with a P-P distance of $2 \cdot 190$ (1) $\AA$. The mean terminal P-O distance is $1.506(2) \AA$ while the terminal $\mathrm{P}-\mathrm{O}(\mathrm{H})$ distance is $1.588(2) \AA$. The pyrophosphate ion also has $C_{2}$ symmetry. The bridge P-O-P bonds make an angle of 136.1 (1) ${ }^{\circ}$ and the $\mathrm{P}-\mathrm{O}$ (bridge) distance is 1.598 (1) $\AA$. The mean value of the terminal P-O distance is 1.494 (2) $\AA$ while the terminal $\mathrm{P}-\mathrm{O}(\mathrm{H})$ distance is 1.569 (2) $\AA$. The bridge oxygen atom of the pyrophosphate is not involved in any appreciable intermolecular bonding and the packing of the ions is similar in both structures.


## Introduction

The unit-cell dimensions and space groups for a number of hydrated sodium hypophosphate and pyrophosphate salts have been reported by Corbridge (1957). In both the tetrasodium decahydrate and disodium dihydrogen hexahydrate series the hypophosphate salt (containing a phosphorus-phosphorus bond) and the pyrophosphate salt (containing a phos-phorus-oxygen-phosphorus bridge) have the same space group and similar unit-cell dimensions. Cor-
bridge suggested that these two hypophosphate-pyrophosphate salt pairs were isomorphous and interpreted his preliminary $b$ axis projections in the disodium dihydrogen series to indicate that the $\mathrm{P}-\mathrm{O}-\mathrm{P}$ bond in the pyrophosphate was linear with the oxygen atom either on a twofold axis or at a center of symmetry. He found the $P-P$ bond in the hypophosphate to be in a similar orientation.

We have determined the crystal structures with diffractometer data of both the disodium dihydrogen hypophosphate hexahydrate $\left(\mathrm{Na}_{2} \mathrm{H}_{2} \mathrm{P}_{2} \mathrm{O}_{6} \cdot 6 \mathrm{H}_{2} \mathrm{O}\right)$ and

